

# Concentration and Temperature Dependence on Diffusivities of CO<sub>2</sub> and N<sub>2</sub> for Poly(dimethyl, methylphenyl siloxane)

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*Experimental determination of solubility and diffusion coefficients of CO<sub>2</sub> and N<sub>2</sub> in poly(dimethyl, methylphenyl siloxane) (PMPS) for the pressure range 0–150 kPa and the temperature range of –10°C to 45°C is discussed. The absorption isotherms were measured by pressure decay equilibrium. Diffusion coefficients were determined by modeling the transient absorption data by Fickian diffusion. The value of solubility coefficient for CO<sub>2</sub> at 35°C was  $1.21 \pm 0.02 \text{ cm}^3 \text{ CO}_2 \text{ (STP)}/(\text{cm}^3 \text{ polymer.atm})$  and it increased to  $2.07 \pm 0.01 \text{ cm}^3 \text{ CO}_2 \text{ (STP)}/(\text{cm}^3 \text{ polymer.atm})$  at 1°C. The absorption isotherms of CO<sub>2</sub> obtained were linear for the pressure range 0–200 kPa and the enthalpy of sorption value was –10.82 kJ/mole for CO<sub>2</sub>. However, the diffusion coefficients of CO<sub>2</sub> changed with feed pressure. The diffusion coefficient of CO<sub>2</sub> in PMPS at 22°C and 128.6 kPa equilibrium pressure was  $7.22 \times 10^{-6} \text{ cm}^2/\text{s}$  and thus the permeability value at these conditions was 1392 Barrers. The diffusion coefficients of CO<sub>2</sub> at 0°C and equilibrium pressures of 125.8 kPa and 10.5 kPa were  $5.72 \times 10^{-6} \text{ cm}^2/\text{s}$  and  $4.31 \times 10^{-6} \text{ cm}^2/\text{s}$ , respectively. Consequently, the CO<sub>2</sub> permeability in PMPS decreases by about 20% when the pressure is reduced from 125.8 to 10.5 kPa at 0°C.*

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## Introduction

This article describes the experimental determination of absorption and diffusion coefficients of pure CO<sub>2</sub> and N<sub>2</sub> as a function of temperature and pressure for poly(dimethyl, methylphenyl siloxane) (PMPS). An interesting behavior in the pure CO<sub>2</sub> permeability was observed for the experiments performed in the pressure range 0–150 kPa.<sup>1</sup> The CO<sub>2</sub> permeability increased as the membrane temperature was reduced from 22°C to –20°C for feed pressures above 50 kPa, but a reversal in trend was observed for feed pressures below 50 kPa. Consequently, there was a decrease in

the CO<sub>2</sub> permeability as the feed pressure was reduced. Also the decrease in the CO<sub>2</sub> permeability with pressure at lower temperatures is larger than at higher temperatures. The possible reasons for this unusual behavior of CO<sub>2</sub> permeability were sought in this study. However, the pure gas N<sub>2</sub> permeability was independent of the feed pressure. This leads to a reduction in the CO<sub>2</sub>/N<sub>2</sub> separation factor at low feed pressures. Similar observations were also made for poly(dimethyl siloxane) (PDMS) membrane.<sup>1,2</sup> The increase in CO<sub>2</sub> permeability with decrease in membrane temperature for PBMS membrane at high feed pressures has been reported by Stern et al.<sup>3</sup> The gas separation application, these membranes were tested for, requires separating CO<sub>2</sub> from N<sub>2</sub>, Ar and traces of other gases (CH<sub>4</sub>, H<sub>2</sub>O) on the Martian surface. Therefore, the membranes were tested over the temperature range –40°C to 10°C and feed pressure range of 5–100 kPa as

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these conditions resemble closely to that in the Martian atmosphere.

The permeability of a gas through a polymer membrane can be defined as the product of solubility and diffusivity of the component. From a simplistic point of view, the variation in permeability can result from changes in either solubility or diffusivity of the component with variation in pressure and temperature. The variation in permeability with temperature is well defined by Arrhenius type behavior as shown in Eq. 4 and, therefore, changes in apparent energy of activation ( $E_p$ ) as a function of pressure can result in different trends in permeability of CO<sub>2</sub> with temperature. The apparent energy of activation is the algebraic sum of energy of activation of diffusion ( $E_d$ ) and enthalpy of absorption ( $\Delta H_s$ ). For condensable CO<sub>2</sub>, the enthalpy of absorption is negative and larger in magnitude than for N<sub>2</sub> and Ar. The reversal in trend is possibly due to a decrease in  $E_d$  as the pressure is increased because of increased polymer chain mobility at high concentration of CO<sub>2</sub> in the polymer. This will result in decrease in the value of  $E_p$  as the concentration is increased and possibly becoming negative at a certain concentration. Therefore, in order to elucidate the trend reversal, it was necessary to experimentally determine the values of  $E_d$  and  $\Delta H_s$  as a function of temperature and pressure.

The equipment design considerations, procedure followed for experimental determination of solubility, and modeling the transient absorption data to determine diffusion coefficients are discussed in this article. The pressure decay method was used to determine the equilibrium absorption of gases in the polymer. The diffusion coefficients were calculated by fitting the transient absorption data, i.e. the mass of gas uptake by the polymer as a function of time, by an appropriate model.<sup>4</sup> The experiments were performed in the temperature range of  $-10^\circ\text{C}$  to  $45^\circ\text{C}$  and pressure range of 0–150 kPa.

## Experimental

### Materials

The copolymer PMPS used in this study was obtained from Dow Corning, product no. 6-3121. NMR analysis of the polymer revealed that there were 90% dimethyl groups and 10% methylphenyl groups on the Si–O backbone of the polymer.<sup>1</sup> The crosslinked density of the polymer was determined to be  $4.38 \times 10^{-4}$  mol/cm<sup>3</sup>.

### Equipment design for absorption measurements

The equipment design is extensively discussed in literature and this apparatus was designed on similar fundamentals.<sup>5,6</sup> However, for our purposes it was important to be able to accurately measure the pressure decay at pressures in the range 5–100 kPa. The overall schematic of the equipment is shown in the Figure 1. The transducers used have a range of 0–666.6 kPa and a resolution of 0.001% of the full-scale reading. The transducers were obtained from MKS instruments, model Baratron Type 627 B. Both the transducers are connected to a power supply and readout, also obtained from MKS instruments model PDR 4000. All the valves are Swagelok manual bellows valves. The system temperature is controlled using a constant temperature water bath. The calibra-

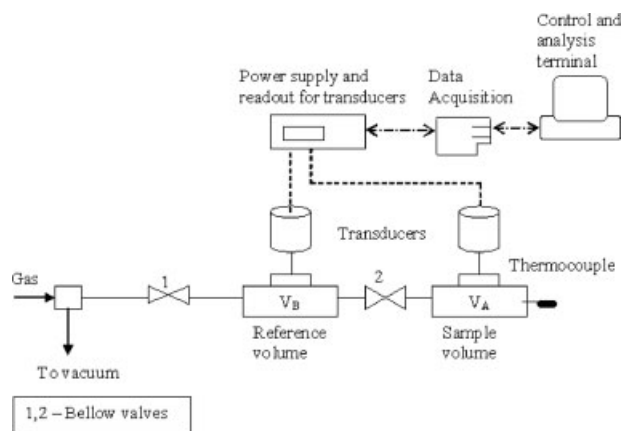


Figure 1. Schematic of the absorption apparatus.

tion of the volumes was performed by helium expansion as described in the literature.<sup>5,6</sup> The calibrated values for the volumes  $V_A$  and  $V_B$  were 24.67 and 24.90 cm<sup>3</sup>, respectively.

### Experimental procedure to determine absorption

The operation of the apparatus to determine the absorption is as follows; the polymer sample is kept in volume  $V_A$  and the volumes  $V_A$  and  $V_B$  are evacuated ( $5.3 \times 10^{-3}$  kPa). Pure gas is expanded in  $V_B$  to the desired pressure through valve 1. The pressure is measured by the transducer and transferred to the computer interface. The valve 1 is closed at the desired pressure in  $V_B$ . Using an appropriate equation of state the number of moles of gas in a given volume can be calculated. The valve 2 is now opened to allow some gas to be expanded into volume  $V_A$ . The number of moles of gas expanded can be calculated from the initial and final pressures in the volume,  $V_B$ . The pressure then decays in the volume containing the polymer,  $V_A$ . By monitoring the pressure decay, the equilibrium pressure can be determined. After pressure equilibrium is reached, the total pressure in  $V_A$  can be used to calculate the moles of gas phase in  $V_A$ . The difference between the moles in the gas phase and the moles transferred from  $V_B$  gives the moles of gas absorbed. The gas compressibility factors ( $z$ ) were calculated using the Redlich Kwong Soave equation of state and the absorption calculations were performed using the compressibility factor equation of state. The polymer sample used is a membrane of PMPS with a uniform thickness of 140  $\mu\text{m}$ . The volume of the sample is 1.26 cm<sup>3</sup>.

### Experimental procedure to determine diffusion coefficients

The experimental measurement of pressure decay vs. time was performed by incorporating a LabVIEW interface with the pressure transducers. The volume  $V_B$  is pressurized to the desired value through valve 1. The valve 1 is closed and pressure is allowed to stabilize in  $V_B$ . The gas is expanded in volume  $V_A$  through valve 2. The pressure decay is measured as a function of time through the LabVIEW interface. The data are collected in the form of pressure vs. time. The difference in two successive pressure readings is converted to moles of gas at STP conditions by an appropriate equation of

state, which accounts for the moles absorbed by the polymer sample at the corresponding time. The plot of total moles uptake with time is fit to a diffusion model to determine the diffusion coefficients. The approach for the model used here is similar to discussed by Crank for diffusion through a stirred solution in limited volume.<sup>7</sup>

## Theory

The product of diffusivity ( $D$ ) and solubility coefficient ( $S$ ) is defined as the permeability ( $P$ ) of a component diffusing through a membrane.

$$P = DS \quad (1)$$

The diffusivity and solubility dependence on temperature is shown by Eqs. 2 and 3.  $\Delta H_s$  is the enthalpy of sorption and  $E_d$  is the activation energy for diffusion. Combining Eqs. 1–3, the temperature dependence of permeability can be defined by Eq. 4 with apparent energy of activation ( $E_p$ ) written as the algebraic sum of activation energy of diffusion and enthalpy of sorption (Eq. 5).

$$S = S_0 \exp\left(\frac{-\Delta H_s}{RT}\right) \quad (2)$$

$$D = D_0 \exp\left(-\frac{E_d}{RT}\right) \quad (3)$$

$$P = P_0 \exp\left(-\frac{E_p}{RT}\right) \quad (4)$$

$$E_p = E_d + \Delta H_s \quad (5)$$

The model to determine diffusion coefficients is as follows; an infinite sheet of thickness  $2l$  is placed in a finite volume of gas and there is diffusion of gas in the sheet. The sheet occupies the space  $-l \leq x \leq l$  and the absorbing gas occupies  $-a - l \leq x \leq l + a$ . The sheet is initially free of gas and the initial concentration of the gas in the volume is  $C_0$ .

The model is given by Eqs. 6 and 7.

$$\frac{M_t}{M_\infty} = 1 - \sum_{n=1}^{\infty} \frac{2\alpha(1+\alpha)}{(1+\alpha+\alpha^2 q_n^2)} \exp\left(-\frac{D q_n^2 t}{l^2}\right) \quad (6)$$

$$\tan q_n l = -\alpha q_n \quad (7)$$

$M_t$  is the total amount of gas dissolved in the polymer at time  $t$  and  $M_\infty$  is the amount of gas dissolved at infinite time or equilibrium absorption. The  $q_n$ 's are the real positive roots of Eq. 7 and  $\alpha = a/Kl$ , which can also be written as  $\alpha = V_g/(KV_p)$ .  $V_p$  and  $V_g$  are polymer and gas volumes, respectively, and  $K$  is the partition coefficient between the polymer and gas phase.

Equation 6 is used to fit the experimental data to determine diffusion coefficients.

The absorption of gases and vapors in crosslinked rubbery polymer is described by the Flory–Rehner expression shown in Eq. 8,<sup>8</sup> where,  $p$  is the pressure of the penetrant,  $p_s$  is the saturation pressure of the penetrant at the temperature,  $\chi$  is the interaction parameter of the penetrant–polymer system,  $\phi_2$  is the penetrant volume fraction in the polymer,  $V_2$  is the

penetrant molar volume and  $v_e/V_0$  is the effective number of crosslinks per unit volume of polymer (moles/volume).

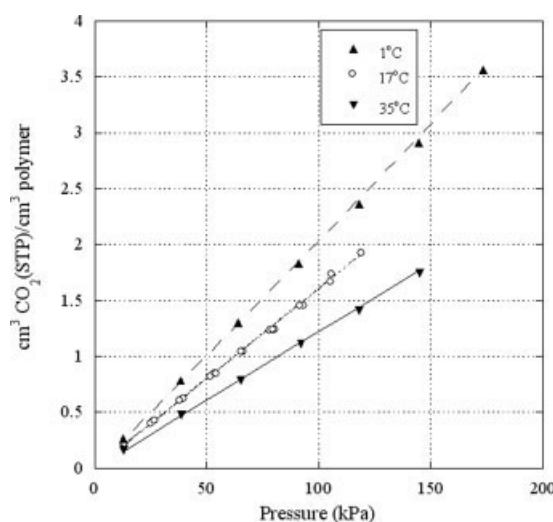
$$\ln\left(\frac{p}{p_s}\right) = \ln \phi_2 + (1 - \phi_2) + \chi(1 - \phi_2)^2 + V_2 \left(\frac{V_e}{V_0}\right) \left[ (1 - \phi_2)^{1/3} - \left(\frac{1 - \phi_2}{2}\right) \right] \quad (8)$$

The volume fraction of the absorbed penetrant is given by Eq. 9, where  $C$  is the equilibrium concentration of the penetrant ( $\text{cm}^3 \text{ gas(STP)}/\text{cm}^3 \text{ polymer}$ ) and  $V_2$  is the penetrant partial molar volume ( $\text{cm}^3/\text{mol}$ ). The interaction parameter could be a function of both temperature and concentration of the penetrant.

$$\phi_2 = \left[ 1 + \frac{22414}{CV_2} \right]^{-1} \quad (9)$$

## Results and Discussion

The absorption isotherms were obtained at five different temperatures in the temperature range 0–35°C. As shown in Figure 2, the absorption isotherms are linear in this pressure range (0–150 kPa). This agrees well with the fact that PMPS is a rubbery polymer and should follow Henry's sorption at these pressure conditions. The absorption isotherms are modeled using the Flory–Rehner expression (Eqs. 8 and 9). The value for the crosslinked density for the PMPS membrane determined by rheology experiments is  $4.38 \times 10^{-4} \text{ mol}/\text{cm}^3$ . The value for the partial molar volume of  $\text{CO}_2$  in PMPS used was  $45 \text{ cm}^3/\text{mol}$ .<sup>9</sup> Table 1 shows the solubility values and the interaction parameter ( $\chi$ ) values for  $\text{CO}_2$  in PMPS as a function of temperature. The interaction parameter values for  $\text{CO}_2$  in PMPS increase as the temperature is decreased. Kamiya et al. have reported the interaction parameter for  $\text{CO}_2$  in PDMS to be 0.73 at 25°C, and also observed an increase in the interaction parameter value with decrease-



**Figure 2. Absorption isotherms for  $\text{CO}_2$  in poly(dimethyl, methylphenyl siloxane).**

The data are modeled using the Flory–Rehner expression for gas absorption in rubbery polymers.

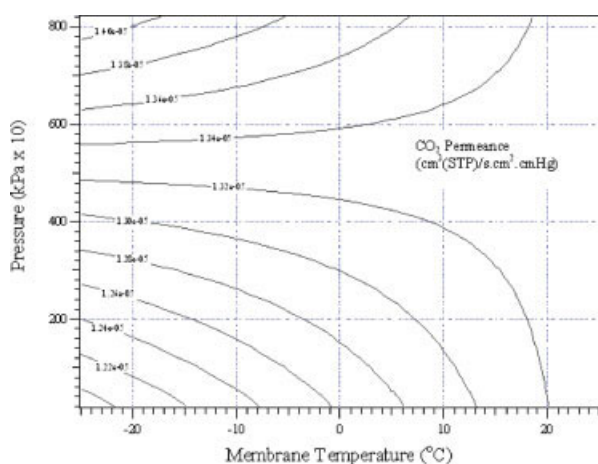
**Table 1. Gas Solubilities and Interaction Parameter Values for the PMPS as a Function of Temperature**

Gas	Temperature (°C)	Solubility Coefficient (cm <sup>3</sup> (STP)/cm <sup>3</sup> Polymer.atm)	Interaction Parameter
CO <sub>2</sub>	1	2.07 ± 0.01	0.90
CO <sub>2</sub>	17	1.61 ± 0.02	0.76
CO <sub>2</sub>	35	1.21 ± 0.02	0.67
N <sub>2</sub>	35	0.10 ± 0.01	—

ing temperature.<sup>10</sup> The enthalpy of absorption ( $\Delta H_s$ ) for CO<sub>2</sub> was calculated to be  $-10.18$  kJ/mole.

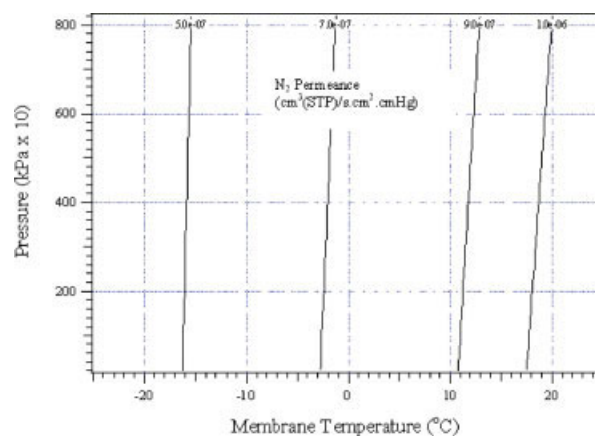
The permeation results of CO<sub>2</sub> for the pressure range 0–80 kPa and temperature range of  $-20^\circ\text{C}$  to  $20^\circ\text{C}$  for PMPS membrane are shown in Figure 3. Figure 4 represents the N<sub>2</sub> permeance results for the above-mentioned conditions. Comparing the isoperms (equal permeance lines) for CO<sub>2</sub> and N<sub>2</sub>, it was observed that the permeance of N<sub>2</sub> remains constant with increase in feed pressure whereas the CO<sub>2</sub> permeance changes significantly with pressure. Also, different trends in the CO<sub>2</sub> permeance can be observed with a variation in membrane temperature. Similar effects have been reported in the literature for the permeability of NH<sub>3</sub> in poly(metasilphenylene siloxane) and for the permeability of propane in a series of side chain and backbone modified siloxane polymers.<sup>3,11</sup> The permeability of NH<sub>3</sub> increases with increasing temperature for low feed pressures (0–2000 mbar) and a reversal in trend occurs at high pressures (500–700 kPa).<sup>11</sup> This polymer has a phenyl group in the backbone and, therefore, is more rigid than PDMS and PMPS, and NH<sub>3</sub> is more condensable than CO<sub>2</sub>. Both these reasons contribute to the fact that the reversal in trend occurs at higher pressures for a more rigid polymer.

The linearity of the absorption isotherms suggests that the change in CO<sub>2</sub> permeability as a function of pressure is due to changes in the diffusion coefficient. Diffusion coefficients were determined by fitting the transient absorption data with the model. The details of the experimental procedure and



**Figure 3. Effect of pressure and temperature on CO<sub>2</sub> permeance for PMPS membrane at low pressure conditions.**

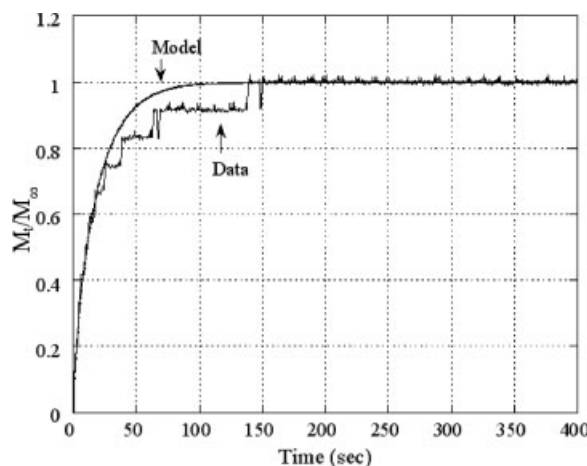
[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]



**Figure 4. Effect of pressure and temperature on N<sub>2</sub> permeance for PMPS membrane at low pressure conditions.**

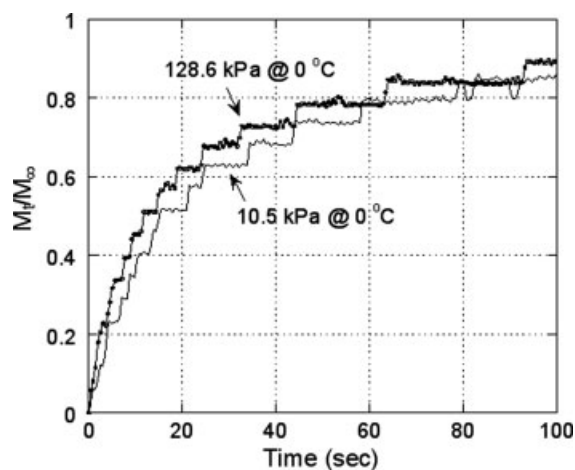
[Color figure can be viewed in the online issue, which is available at [www.interscience.wiley.com](http://www.interscience.wiley.com).]

modeling are discussed earlier in the Experimental procedure to determine absorption sections and Theory section. Equations 6 and 7 were used to fit the data to determine the diffusion coefficients. The value of  $\alpha$  was calculated from known volumes of polymer and gas phase, and the partition coefficient of the gas at the particular temperature. The first five terms ( $n$  values 1–5) in Eq. 6 were used to fit the data. Figure 5 presents the transient absorption data for an equilibrium pressure of 28.1 kPa at  $23^\circ\text{C}$  in which the ordinate represents mass uptake of the gas at any time ( $t$ ) normalized by equilibrium mass uptake ( $M_t/M_\infty$ ) and abscissa represents the time. The curve representing the model is also depicted in this Figure. The least squares method was used to fit the data to the model. The diffusion coefficient obtained from fitting the data with the model was  $6.71 \times 10^{-6}$  cm<sup>2</sup>/s with the permeability value of 1295 Barrers. The value of the diffusion coefficient at 128.6 kPa equilibrium pressure and  $23^\circ\text{C}$  was



**Figure 5. CO<sub>2</sub> transient absorption data and model in poly(dimethyl, methylphenyl siloxane) at 28.1 kPa equilibrium pressure and  $22^\circ\text{C}$ .**





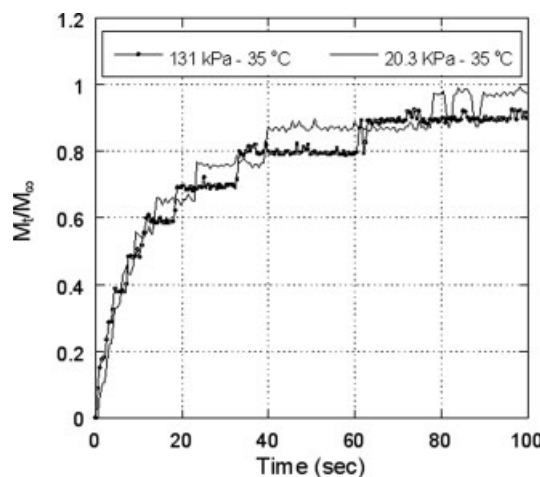
**Figure 6.** CO<sub>2</sub> transient absorption data at 0°C and equilibrium pressures of 10.5 kPa and 125.8 kPa.

$7.22 \times 10^{-6}$  cm<sup>2</sup>/s with the permeability value of 1392 Barrers. The value of the permeability calculated from steady state permeation experiment is 1470 Barrers at 137.8 kPa differential pressure and 21°C,<sup>1</sup> which is within 10% of the value obtained from the absorption measurement. A more significant reduction in the diffusion coefficient with a decrease in pressure was observed at lower membrane temperatures. Figure 6 shows  $M_t/M_\infty$  vs. time at 0°C for equilibrium pressures of 10.5 kPa and 125.8 kPa. The value of the diffusion coefficients at 125.8 kPa and 10.5 kPa were  $5.72 \times 10^{-6}$  cm<sup>2</sup>/s and  $4.31 \times 10^{-6}$  cm<sup>2</sup>/s, respectively; a significant difference in values. These diffusion coefficient values are lower than the value obtained at 23°C, which is expected as the diffusion coefficients of gases in polymers decrease with a decrease in temperature. Table 2 shows the diffusion coefficients of CO<sub>2</sub> in PMPS at various temperatures and pressures.

**Table 2.** Diffusion Coefficients of CO<sub>2</sub> in PMPS at Various Temperatures and Pressures

Temperature (°C)	Pressure (mbar)	Diffusion Coefficient $\times 10^6$ (cm <sup>2</sup> /s)	$R^2$
0	105.00	4.31	0.95
	149.00	4.52	0.94
	151.00	4.59	0.94
	629.00	5.11	0.93
	1258.0	5.72	0.92
23	1919.0	5.75	0.92
	281.00	6.71	0.93
	544.00	6.79	0.92
	1286.0	7.22	0.93
	2000.0	7.22	0.91
35	203.00	7.73	0.93
	1310.0	7.80	0.94
45	490.00	8.52	0.95
	1306.0	8.51	0.92
	1882.0	8.52	0.92

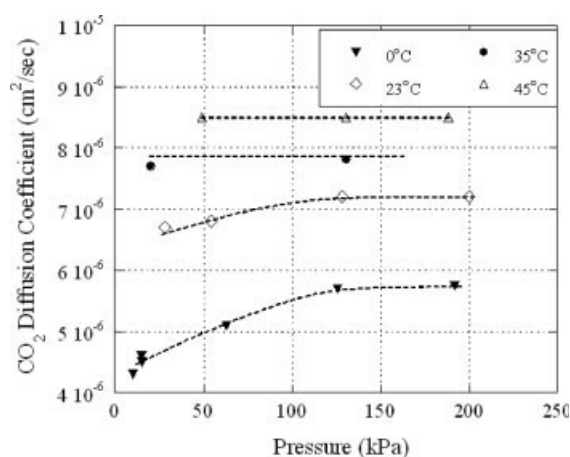
$R^2$  values are from the least sum of squares regression fit of the model to the transient absorption data.



**Figure 7.** CO<sub>2</sub> transient absorption data at 0°C – 125.8 kPa and 45°C – 130.6 kPa.

As the membrane temperature is increased further, i.e. at 35°C, the diffusion coefficients become independent of pressure. Figure 7 represents the transient absorption data at 35°C for equilibrium pressures of 20.3 and 131.0 kPa, and the diffusion coefficient value in both cases is  $\sim 7.8 \times 10^{-6}$  cm<sup>2</sup>/s. Figure 8 depicts the diffusion coefficients of CO<sub>2</sub> calculated from transient absorption data vs. equilibrium pressure at different temperatures. In general, the diffusion coefficients decrease as the membrane temperature is reduced at all pressures. At lower membrane temperatures, the diffusion coefficients also decrease as the pressure is reduced. The reduction in the diffusion coefficient with feed pressure was larger at 0°C than at 23°C.

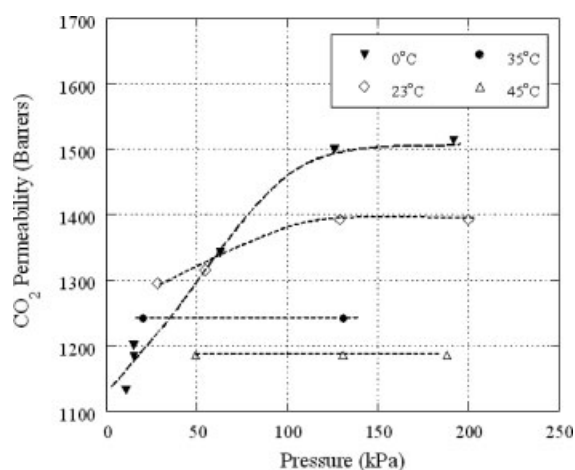
The changes in CO<sub>2</sub> permeability and diffusion coefficient as a function of pressure can be related to CO<sub>2</sub> induced structural changes in the polymer as the concentration of the gas in the polymer increases with increasing pressures. It is important to note that only the diffusion coefficients are affected with pressure and not the absorption isotherms that



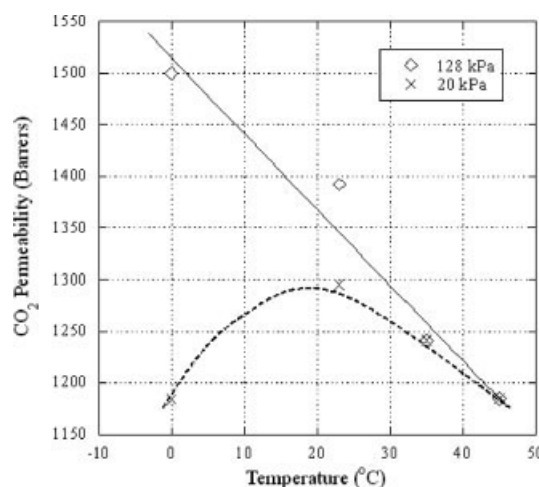
**Figure 8.** Diffusion coefficients of CO<sub>2</sub> in PMPS calculated from transient absorption data vs. equilibrium pressure at different temperatures.

are observed to be linear for this pressure range. As the feed pressure was increased at 0°C, the diffusion coefficient approached a constant value of  $\sim 5.75 \times 10^{-6} \text{ cm}^2/\text{s}$ . As the membrane temperature was increased, apparently the effect of  $\text{CO}_2$  induced structural changes leading to an effect on the diffusion coefficient diminishes. It was observed that the diffusion coefficients ( $\text{CO}_2$ ) were independent of pressure above 35°C. The diffusion coefficients becoming independent of the pressure at high temperature is a condition that can be thought to be analogous to the observation where the diffusion coefficients approach a constant value at higher pressures for 0°C. The free volume of the polymer is increased at higher temperatures due to increased chain motions. This may be the reason that the dissolved  $\text{CO}_2$  does not cause significant structural changes to the polymer, which is already in an expanded state. Also, at temperatures 0 and 23°C, the polymer reaches a limit where further increment in the concentration of  $\text{CO}_2$  in the polymer does not lead to an increase in the diffusion coefficient. Moreover, the amount of gas dissolved in the polymer at a particular pressure increases as the polymer temperature is reduced which further supports plasticization of polymer at lower temperatures that affects the diffusion coefficient. This effect becomes more prominent at lower temperatures and high pressures. For low feed pressures, the amount of gas dissolved in the polymer is low and doesn't produce significant effects on the diffusion coefficient of  $\text{CO}_2$ .

Figure 9 shows the variation in permeability vs. the pressure at different temperatures calculated from absorption measurements. The permeability of  $\text{CO}_2$  decreased with an increase in temperature for pressures above 70 kPa and for all temperatures (0–45°C). The permeability was observed to increase with increase in temperature for pressures below 50 kPa for the temperature range of 0 to 25°C. At temperatures above 25°C, there was not any significant pressure dependence on  $\text{CO}_2$  permeability and the permeability decreased with an increase in the membrane temperature. The  $\text{CO}_2$  permeability as a function of temperature for feed pressures of 128 and 20 kPa is shown in Figure 10. This Figure depicts the  $\text{CO}_2$  permeability reaching a maximum for



**Figure 9.**  $\text{CO}_2$  permeability in PMPS calculated from transient absorption data vs. equilibrium pressure at different temperatures.



**Figure 10.**  $\text{CO}_2$  permeability in PMPS calculated from transient absorption data vs. temperature at 128 and 20 kPa equilibrium pressures.

low pressure whereas there is a constant decline in permeability at high pressures. The  $\text{CO}_2$  permeability at 0°C increases from about 1200 Barrers at 15 kPa to 1500 Barrers at 126 kPa. Figure 5 represents the gas permeation results with the PMPS membrane obtained at Lockheed Martin under simulated Martian atmospheric conditions. In this Figure, the  $\text{CO}_2$  permeance at 0°C and 15 kPa feed pressure is approximately  $1.25 \times 10^{-6} \text{ cm}^3(\text{STP})/\text{cm}^2\text{s.cm Hg}$  which increases to  $1.37 \times 10^{-6} \text{ cm}^3(\text{STP})/\text{cm}^2\text{s.cm Hg}$  at 80 kPa. This is about a 10% increase in permeance as the feed pressure. The increase in  $\text{CO}_2$  permeability determined by absorption experiments from 15 to 80 kPa at 0°C computed from Figure 9 is  $\sim 15\%$ , which agrees closely with the increase in permeance at these conditions discussed earlier. The nitrogen absorption isotherm at 23°C was obtained in the pressure range 0–200 kPa and was found to be linear. The solubility coefficient value at 23°C for  $\text{N}_2$  in PMPS was calculated to be  $0.12 \text{ cm}^3(\text{STP})/(\text{cm}^3 \text{ polymer.atm})$ . The diffusion coefficient of  $\text{N}_2$  computed from the transient absorption data at 23°C and 211 kPa equilibrium pressure was  $9.10 \times 10^{-6} \text{ cm}^2/\text{s}$ . This value is higher than the diffusion coefficient of  $\text{CO}_2$  in PMPS, which is  $7.22 \times 10^{-6} \text{ cm}^2/\text{s}$  at 23°C and 126 kPa equilibrium pressure. Merkel et al., have reported diffusion coefficients of  $\text{CO}_2$  and  $\text{N}_2$  in PDMS. The diffusion coefficient values of  $\text{CO}_2$  and  $\text{N}_2$  reported were  $22 \times 10^{-6} \text{ cm}^2/\text{s}$  and  $34 \times 10^{-6} \text{ cm}^2/\text{s}$ , respectively at 35°C.<sup>8</sup> PMPS has 90% dimethyl groups and 10% methylphenyl groups on the backbone, so the polymer could have similar gas transport properties as PDMS, as seen in this case where the diffusion coefficient of  $\text{N}_2$  is higher than  $\text{CO}_2$  in both polymers. However, PMPS has 10% methylphenyl groups that make the structure of the polymer more rigid than PDMS and could be the primary reason for the lower diffusion coefficients of  $\text{CO}_2$  and  $\text{N}_2$  in PMPS as compared with PDMS. Also, a more rigid structure would favor diffusivity selectivity of  $\text{CO}_2$  over  $\text{N}_2$  as more energy would be required for diffusional jump for  $\text{N}_2$  in PMPS than in PDMS because of its larger kinetic diameter. In essence, if the structural rigidity of the polymer is increased, the diffusion coefficient of  $\text{N}_2$  could become less than  $\text{CO}_2$ . The diffusion coefficient

was found to be independent of pressure for N<sub>2</sub> in PMPS and absorption isotherms were linear with pressure; this observation is in good agreement with that seen in Figure 4 where the N<sub>2</sub> permeances are constant with pressure.

## Conclusions

This study was intended to explain the transport behavior of CO<sub>2</sub> through rubbery PMPS at low temperature and low pressure conditions. The absorption isotherms were measured by pressure decay equilibrium and the diffusion coefficients were determined by model fits to the transient absorption data for CO<sub>2</sub> and N<sub>2</sub>. The absorption isotherms were found to be linear for both gases in the pressure range 0–200 kPa and for temperatures in the range 0–35°C. However, the diffusion coefficient of CO<sub>2</sub> was found to be a function of feed pressure for temperatures below 25°C. The CO<sub>2</sub> diffusion coefficient increased from  $4.52 \times 10^{-6}$  cm<sup>2</sup>/s at 15 kPa to  $5.72 \times 10^{-6}$  cm<sup>2</sup>/s at 125.8 kPa for the sample temperature of 0°C. Therefore, it is primarily the reason for change in permeability of CO<sub>2</sub> with pressure. The change in CO<sub>2</sub> permeability is larger at lower temperatures. The reversal in the trend of CO<sub>2</sub> permeability with temperature as the feed pressure is increased is also explained. The increase in diffusion coefficients as the pressure is increased at low temperature is larger than at high temperature. Because of this effect on the diffusion coefficient, the permeability shows varying trends with temperature at different feed pressures. In contrast, the N<sub>2</sub> permeability is not affected by feed pressure.

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